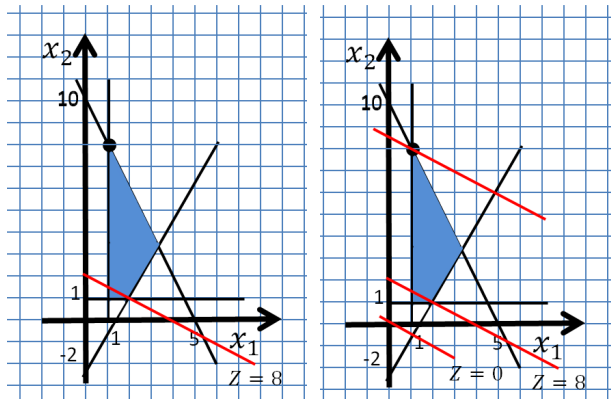


1.a)

$x_1$  Tones of C1 to produce weekly

$x_2$  Tones of C2 to produce weekly

1.b) and 1.c)  $8 = 2x_1 + 4x_2$       1.d)  $\begin{cases} x_1 = 1 \\ 2x_1 + x_2 = 10 \end{cases} \Rightarrow \begin{cases} x_1 = 1 \\ x_2 = 8 \end{cases} \Rightarrow z = 34$



1.e) A: BNFS; B: NBNFS; C: BFS optimal; D: NBFS.

f)  $Min W = 10y_1 + 2y_2 + y_3 + y_4$

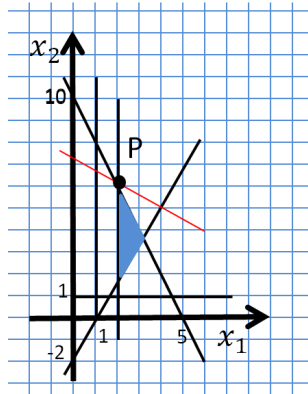
$$s. t. \begin{cases} 2y_1 + 2y_2 + y_3 \geq 2 \\ y_1 - y_2 + y_4 \geq 4 \\ y_1, y_2 \geq 0 \\ y_3, y_4 \leq 0 \end{cases}$$

g)  $y_3 = \Delta Z$  if  $\Delta b_3 = +1$

New problem:

$$Max Z = 2x_1 + 4x_2$$

$$s. t. \begin{cases} 2x_1 + x_2 \leq 10 \\ 2x_1 - x_2 \leq 2 \\ x_1 \geq 2 \\ x_2 \geq 1 \\ x_1, x_2 \geq 0 \end{cases}$$



New optimal solution: point P

$$\begin{cases} x_1 = 2 \\ 2x_1 + x_2 = 8 \end{cases} \quad (\dots) \quad \begin{cases} x_1 = 2 \\ x_2 = 6 \end{cases} \Rightarrow \text{Novo } z = 28$$

$y_3 = \Delta Z = 28 - 34 = -6$ ;  $y_3 = -6 \leq 0$  This is accordingly to the dual

$y_3$ : Each unit of C1 that the company is forced to produce above (below) the current minimum required (that is one unit), the profit decreases (increases) 6 m. u. ( $= -y_3$ ), while the optimal basis is maintained.

2. a)

	Z	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	RHS
z	1	0	0	0	-4	-1	6
$x_1$	0	1	0	0	0	-1/5	1
$x_3$	0	0	0	1	2	3/5	6
$x_2$	0	0	1	0	2	3/5	4
z	1	0	2	0	0	1/5	14
$x_1$	0	1	0	0	0	-1/5	1
$x_3$	0	0	-1	1	0	0	2
$x_4$	0	0	1/2	0	1	3/10	2

**Entering criteria**

$$\text{Min}\{-4, -1\} = -4$$

$x_4$  new basic

**Leaving criteria**

$$\text{Min}\left\{\frac{6}{2}, \frac{4}{2}\right\} = 2$$

$x_2$  new non basic

b)  $x = (1,0,2,2,0)$ . Optimal BFS.